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% Performs rotations of Cartesian representations of spin interaction
% tensors by the user-supplied Euler angles.
%
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function inter_tensor=rotate_interaction(inter_tensor,alpha,beta,gamma)

% Gamma rotation in XY plane
R_gamma=[cos(gamma) -sin(gamma) 0;
          sin(gamma) cos(gamma) 0;
          0           0           1];

% Beta rotation in YZ plane
R_beta=[1           0           0;
          0           cos(beta) -sin(beta);
          0           sin(beta) cos(beta)];

% Alpha rotation in XY plane
R_alpha=[cos(alpha) -sin(alpha) 0;
          sin(alpha) cos(alpha) 0;
          0           0           1];

% The total rotation
R=R_alpha*R_beta*R_gamma;

% Apply rotation to the interaction
inter_tensor=R*inter_tensor*R';

end
```

```
% Basic 14N axial quadrupolar powder pattern.  
%  
% i.kuprov@soton.ac.uk  
  
function hello_world()  
  
% Pauli matrices for spin-1 particle  
sigma_x=[0 1 0; 1 0 1; 0 1 0]/sqrt(2);  
sigma_y=[0 -1i 0; 1i 0 -1i; 0 1i 0]/sqrt(2);  
sigma_z=[1 0 0; 0 0 0; 0 0 -1];  
  
% Isotropic Zeeman interaction  
omega_zeeman=2*pi*1000;  
  
% Quadrupolar tensor (must be axial - phi averaging not done)  
quad_tensor=2*pi*[-5e2 0 0  
                    0 -5e2 0  
                    0 0 1e3];  
  
% Isotropic Hamiltonian  
H=omega_zeeman*sigma_z;  
  
% Timing and detection parameters  
time_step=1e-4; coil=sigma_x+1i*sigma_y;  
  
% Preallocate the fid  
fid=zeros(1,500);  
  
% Loop over theta only  
for theta=linspace(0,pi,500);  
  
    % Compute grid weight  
    weight=sin(theta)/500;  
  
    % Rotate quadrupolar tensor into current orientation  
    current_quad=rotate_interaction(quad_tensor,0,theta,0);  
  
    % Create current orientation Hamiltonian  
    H_current=H+(current_quad(3,3)-0.5*(current_quad(1,1)+current_quad(2,2)))*...  
                (2/3)*(sigma_z^2-0.5*(sigma_x^2+sigma_y^2));  
  
    % Initial condition  
    rho=sigma_x;  
  
    % Compute the propagator  
    P=expm(-1i*H_current*time_step);  
  
    % Run time evolution  
    for n=1:500  
        fid(n)=fid(n)+weight*trace(coil'*rho);  
        rho=P'*rho*P;  
    end  
  
end
```

```
% Apodization
fid=fid.*exp(-10*linspace(0,1,numel(fid)));
% Plotting
plot(real(fftshift(fft(fid))));
```

```
end
```

```
% Basic nitroxide radical EPR powder pattern.
%
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function hello_again_world()

% Pauli matrices for spin-1 particle
sigma2_x=[0 1 0; 1 0 1; 0 1 0]/sqrt(2);
sigma2_y=[0 -1i 0; 1i 0 -1i; 0 1i 0]/sqrt(2);
sigma2_z=[1 0 0; 0 0 0; 0 0 -1];

% Pauli matrices for spin-1/2 particle
sigmal_x=[0 1/2; 1/2 0];
sigmal_y=[0 -1i/2; 1i/2 0];
sigmal_z=[1/2 0; 0 -1/2];

% Interactions (must be axial and collinear - phi integration not done)
zeeman_tensor=2*pi*[-1e6 0 0
                      0 -1e6 0
                      0 0 2e6];
hfc_tensor= 2*pi*[-2e6 0 0
                   0 -2e6 0
                   0 0 4e6] + 2*pi*eye(3)*1e6;

% Isotropic Hamiltonian
H=(trace(hfc_tensor)/3)*(kron(sigmal_x,sigma2_x)+...
                           kron(sigmal_y,sigma2_y)+...
                           kron(sigmal_z,sigma2_z));

% Destroy the isotropic part of the hfc tensor (no longer needed)
hfc_tensor=hfc_tensor-eye(3)*trace(hfc_tensor)/3;

% Timing and detection parameters
time_step=6e-8;
coil=kron(sigmal_x,eye(3))+1i*kron(sigmal_y,eye(3));

% Preallocate the fid
fid=zeros(1,500);

% Loop over theta
for theta=linspace(0,pi,500);

    % Compute grid weight
    weight=sin(theta)/500;

    % Rotate interaction tensors into current orientation
    current_hfc=rotate_interaction(hfc_tensor,0,theta,0);
    current_zeeman=rotate_interaction(zeeman_tensor,0,theta,0);

    % Create current orientation Hamiltonian
    H_current=H+current_zeeman(3,3)*kron(sigmal_z,eye(3))+...
               (2/3)*(current_hfc(3,3)-0.5*(current_hfc(1,1)+current_hfc(2,2)))*...
               (kron(sigmal_z,sigma2_z)-0.5*(kron(sigmal_x,sigma2_x)+kron(sigmal_y,%
sigma2_y)));

```

```
% Initial condition
rho=kron(sigma1_x,eye(3));

% Compute the propagator
P=expm(-1i*H_current*time_step);

% Run time evolution
for n=1:500
    fid(n)=fid(n)+weight*trace(coil'*rho);
    rho=P'*rho*P;
end

% end

% Apodization
fid=fid.*exp(-10*linspace(0,1,numel(fid)));

% Plotting
plot(real(fftshift(fft(fid))));

end
```